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## HEAT CAPACITY IN PROTEINS

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■ **Abstract** Heat capacity ( $C_p$ ) is one of several major thermodynamic quantities commonly measured in proteins. With more than half a dozen definitions, it is the hardest of these quantities to understand in physical terms, but the richest in insight. There are many ramifications of observed  $C_p$  changes: The sign distinguishes apolar from polar solvation. It imparts a temperature ( $T$ ) dependence to entropy and enthalpy that may change their signs, and which of them dominate. Protein unfolding usually has a positive  $\Delta C_p$ , producing a maximum in stability and sometimes cold denaturation. There are two heat capacity contributions, from hydration and protein-protein interactions; which dominates in folding and binding is an open question. Theoretical work to date has dealt mostly with the hydration term and can account, at least semi-quantitatively, for the major  $C_p$ -related features: the positive and negative hydration  $C_p$  of hydration for apolar and polar groups, respectively; the convergence of apolar group hydration entropy at  $T \approx 112^\circ\text{C}$ ; the decrease in apolar hydration  $C_p$  with increasing  $T$ ; and the  $T$ -maximum in protein stability and cold denaturation.

### 1. INTRODUCTION

Some of the earliest systematic calorimetric measurements were made by Benjamin Thompson in the 1780s, when he used the increase in temperature of a cask of water to measure the amount of heat produced by boring out cannon barrels. More than two centuries later, the sensitivity of calorimeters is probably a billion-fold higher. Heat changes produced by protein unfolding, protein association, ligand binding, and other protein reactions can now be measured routinely. The two principal instrument modes are differential scanning calorimetry (DSC), which measures sample heat capacity ( $C_p$ ) with respect to a reference as a function of temperature, and isothermal titration calorimetry (ITC), which measures the heat uptake/evolution during a titration experiment. The third major tool is thermodynamic calorimetry, which does not use a calorimeter per se. The temperature dependence of an equilibrium constant, measured using any appropriate method (CD, fluorescence, NMR, etc.), is combined with the van't Hoff relations to obtain enthalpy and heat capacity changes. With these tools at the disposal

of biophysicists and biochemists, the output of heat capacity data on proteins has steadily increased. Most heat capacity data are collected at constant pressure, yielding  $C_p$ . Constant volume heat capacity ( $C_v$ ) data are much rarer in the protein field. In addition, at 1 Atm PV ( $P$  = Pressure,  $V$  = Volume) changes in protein reactions are usually very small compared with  $kT$  (Thermal energy, where  $k$  is the Boltzmann constant, and  $T$  the absolute temperature). In this review, we refer almost exclusively to  $C_p$  and for brevity use enthalpy ( $H$ ) and mean energy ( $E$ ) interchangeably.

$C_p$  is one of the five major thermodynamic quantities commonly tabulated in biophysical studies on proteins; the others are Gibbs free energy ( $G$ ), enthalpy, entropy ( $S$ ), and volume. Of course, these data are not an end in themselves, but they are measured with the aim of providing physical, mechanistic, even atomic level insight into how proteins fold, how they are stabilized, and how they function. In some respects, which we outline below,  $C_p$  is both the richest potential source of this insight and the hardest of the five thermodynamic quantities to understand in physical terms. Volume is by definition a physical quantity and straightforward to understand, although there are some subtleties in defining the volume of a protein in solution. Enthalpy is a direct measure of heat or energy, whereas entropy quantifies the “disorder” or number of configurations available to the system. Free energy has a direct relationship to a primary observable, the equilibrium constant  $K$  through  $\Delta G = -kT \ln K$ , which describes the balance between enthalpy and entropy. In our experience, however, heat capacity is less intuitively understood. Why should one protein or protein state be able to absorb more heat than another for the same increase in  $T$ ? What is the physical origin of  $C_p$  differences? In this review, we first provide a short theoretical overview of heat capacity and then discuss some theoretical and experimental papers. Our goal is not to be exhaustive either in the theoretical overview or in the literature review, but rather to provide, through some background and simple models, physical intuition about  $C_p$  that can be used to parse experimental measurements; to indicate the many potential ramifications of  $C_p$  changes observed in the literature; and to focus on some experimental and theoretical studies that, in our view, elucidate physical origins and fundamental aspects of heat capacity changes in proteins. Space limitations preclude discussion of many studies of particular protein systems and tabulations of heat capacity data. Furthermore, our focus is on physical aspects rather than on applications.

## 2. THEORETICAL OVERVIEW OF HEAT CAPACITY

### 2.1. Definition of Heat Capacity

Heat capacity has more than half a dozen definitions, of which the first is synonymous with its name

$$C_p = \frac{dH}{dT}, \quad 1.$$

i.e., the increase in energy (heat) with temperature. The other three commonly used definitions are

$$C_p = T \frac{dS}{dT} = -T^2 \frac{d^2G}{dT^2} = \frac{\langle \delta H^2 \rangle}{kT^2}, \quad 2.$$

which are, respectively, the temperature dependence of the entropy, the second derivative or curvature of the free energy, and the mean squared fluctuation in energy scaled by  $kT^2$ . Equations 1 and 2 apply also to changes in entropy, enthalpy, and free energy by substituting  $\Delta C_p$ ,  $\Delta H$ ,  $\Delta S$ , and  $\Delta G$ . Equations 1 and 2a together describe how the heat capacity is a measure of the temperature dependent form of entropy/enthalpy compensation. Because  $G = H - TS$  and entropy and enthalpy change in the same direction, free energy has a much weaker dependence on temperature than either of its components has. Heat capacity expressed as the curvature of the free energy means that a positive (negative) change in heat capacity yields a downward (upward) curvature to  $\Delta G$ , and potentially a maximum (minimum) in free energy with  $T$  if the accessible temperature range permits. At this extremum, it follows from  $S = -dG/dT$  that the entropy change is zero. The fourth definition of  $C_p$  (Equation 2c) as the mean squared fluctuation in the enthalpy is, on the face of it, less obvious than the temperature derivative of the enthalpy, but it usually provides the easiest route to a physical interpretation. Because  $C_p$  can be defined in terms of the temperature derivative of both entropy and enthalpy, there is an entropic version of the fluctuation formula:

$$C_p = \frac{\langle \delta S^2 \rangle}{k}. \quad 3.$$

All these definitions are equivalent at a statistical mechanical level. The configurational part of the all-important partition function is

$$Z = \int e^{-U(\mathbf{r})/kT} d\mathbf{r}, \quad 4.$$

where  $U$  is the Hamiltonian or potential energy as a function of the coordinates  $\mathbf{r}$ . The probability of a particular state is

$$p(\mathbf{r}) = e^{-U(\mathbf{r})/kT} / Z. \quad 5.$$

Then the entropy may be written in terms of the famous Boltzmann equation as

$$S/k = - \int p(\mathbf{r}) \ln p(\mathbf{r}) d\mathbf{r} = -\langle \ln p(\mathbf{r}) \rangle, \quad 6.$$

where  $\langle \rangle$  indicates an ensemble average. To extend this to heat capacity, we use the statistical mechanical result that the temperature dependence of the ensemble average of a quantity  $X$  is given by

$$\frac{d\langle X \rangle}{dT} = \frac{1}{kT^2} \langle XU \rangle - \langle X \rangle \langle U \rangle = \frac{1}{kT^2} \langle \delta X \delta U \rangle, \quad 7.$$

the covariance of its fluctuation with the energy fluctuation. Combined with Equations 2a and 5 we obtain the statistical mechanical expression for the heat capacity

$$Cp/k = \langle [\ln p(r)]^2 \rangle - \langle \ln p(r) \rangle^2 = \langle [\delta \ln p(r)]^2 \rangle, \quad 8.$$

as the mean squared fluctuation in log probability (compare also Equations 3 and 6). We note that using  $X = U$  in Equation 7 allows us to derive the aforementioned identity

$$Cp = \frac{dH}{dT} = \frac{\langle \delta H^2 \rangle}{kT^2}, \quad 9.$$

where  $\langle U \rangle = E \approx H$ . Equation 9 is an example of a general relationship in statistical mechanics between a susceptibility of some quantity and the magnitude of the square of the fluctuations in that quantity at equilibrium (1). Lastly, we can use the statistical mechanics relationships to obtain our final expression for the heat capacity

$$Cp = \frac{\langle \delta H \delta S \rangle}{kT}, \quad 10.$$

as the covariance in enthalpy-entropy fluctuations that gives formal expression to the concept of  $Cp$  as a measure of entropy-enthalpy compensation. Interestingly, because  $G = H - TS$ , Equations 2, 3, and 10 tell us that the total fluctuation in free energy is identically zero (2),

$$\begin{aligned} \langle \delta G^2 \rangle &= \langle (\delta H - T \delta S)(\delta H - T \delta S) \rangle \\ &= \langle \delta H^2 \rangle + T^2 \langle \delta S^2 \rangle - 2T \langle \delta H \delta S \rangle = 0. \end{aligned} \quad 11.$$

Which of the seven expressions for heat capacity, Equations 1–3, 8, and 10, one should use depends on several criteria. For the experimentalist, these criteria include how the heat capacity is being measured and what is being deduced from experimental measurements. For the theoretician aiming to calculate heat capacities, these criteria include what theory is being used, and what are the relative numerical difficulties inherent in the different expressions.

Integration of Equations 1 and 2 with the assumption of constant heat capacity leads to the very useful modified Gibbs-Helmholtz, or integrated van't Hoff Equation

$$\Delta H(T) = \Delta H(T^{ref}) + \Delta Cp(T - T^{ref}), \quad 12a.$$

$$\Delta S(T) = \Delta S(T^{ref}) + \Delta Cp \ln(T/T^{ref}), \quad 12b.$$

$$\begin{aligned} \Delta G(T) &= \Delta H(T^{ref}) - T \Delta S(T^{ref}) \\ &+ \Delta Cp[(T - T^{ref}) - T \ln(T/T^{ref})], \end{aligned} \quad 12c.$$

which gives the enthalpy, entropy, and free energy at a particular temperature in

terms of entropy, enthalpy, and heat capacity at a second conveniently chosen reference temperature  $T^{\text{ref}}$ . This Equation is commonly used either to extract enthalpy, entropy, and heat capacity changes from a temperature-dependent series of free energies or equilibrium constants (thermodynamic calorimetry), or to extrapolate protein free energies, stabilities, etc., to various temperatures given values of enthalpy, entropy, and heat capacity at the reference temperature. Many analyses of protein data assume a temperature invariant heat capacity, an assumption that often, but not always, leads to little error (3). However, more extended experimental data sets do provide information on the temperature dependence of the heat capacity (4, 5), and theoretical analyses of the hydrophobic effect are now addressing this higher-order thermodynamic effect (6, 7). Assume a linear dependence of  $\Delta C_p$  on temperature with a coefficient  $D$ ,  $\Delta C_p = \Delta C_p^{\text{ref}} + D(T - T^{\text{ref}})$ . Substituting into Equations 1 and 2a, and integrating with respect to  $T$  gives the next highest order form of the integrated van't Hoff Equation

$$\begin{aligned} \Delta G(T) = & \Delta H(T^{\text{ref}}) - T \Delta S(T^{\text{ref}}) + \Delta C_p^{\text{ref}}[(T - T^{\text{ref}}) - T \ln(T/T^{\text{ref}})] \\ & + D[(T - T^{\text{ref}})^2/2 - T(T - T^{\text{ref}}) + TT^{\text{ref}} \ln(T/T^{\text{ref}})]. \end{aligned} \quad 13.$$

Higher-order forms are easily derived. For example, Brandts (8) found that best fit to Chymotrypsin denaturation data required a T-dependent  $C_p$  model of the form  $\Delta C_p = -2BT - 6CT^2$ , but this order of van't Hoff analysis is the exception rather than the rule due to lack of suitable data.

## 2.2. Simple Models for Interpreting Heat Capacity

Simple thermodynamic models are rarely applicable to protein data when applied literally, but they are often useful for building up intuition about the underlying physical chemistry. The simplest models for looking at heat capacity are the harmonic oscillator and the two-energy-level model. In particular, the two-energy-level model is rich enough to demonstrate most of the physical effects necessary for a qualitative understanding of heat capacity. For a harmonic oscillator with frequency  $\nu$ , the heat capacity is (9)

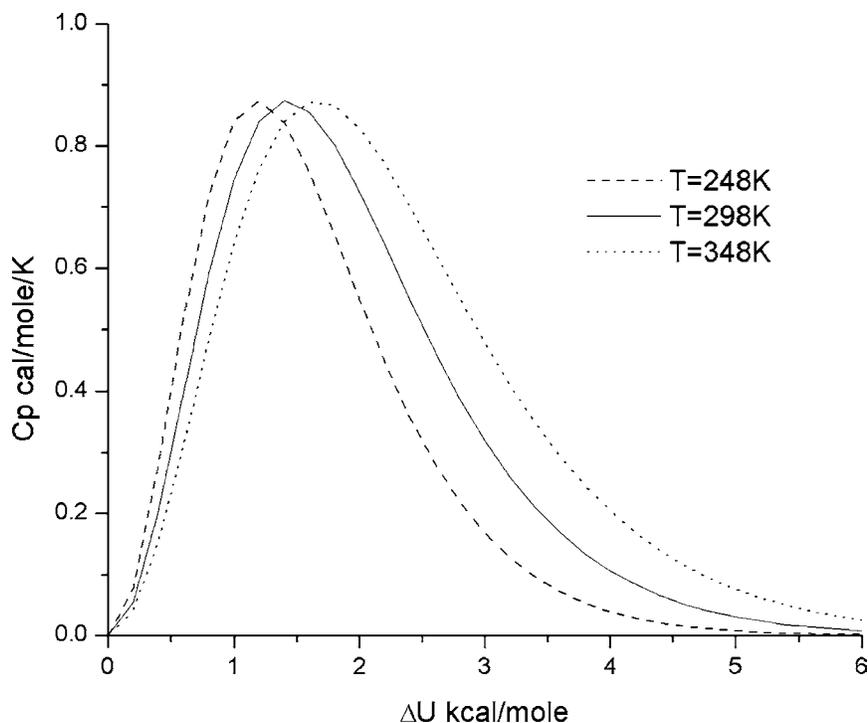
$$C_p = \frac{(h\nu/2kT)^2}{\sinh^2(h\nu/2kT)}, \quad 14.$$

where  $h$  is Planck's constant. For a two-energy-level model, where the two states are separated by an energy of  $\Delta U$ , the heat capacity is easily evaluated using Equation 2c as

$$C_p = \frac{\Delta U^2 e^{-\Delta U/kT}}{kT^2(1 + e^{-\Delta U/kT})^2} = \frac{\Delta U^2}{kT^2} p_0 p_1, \quad 15.$$

where  $p_0$  and  $p_1$  are the probabilities of the system being in the lower and upper states, respectively.





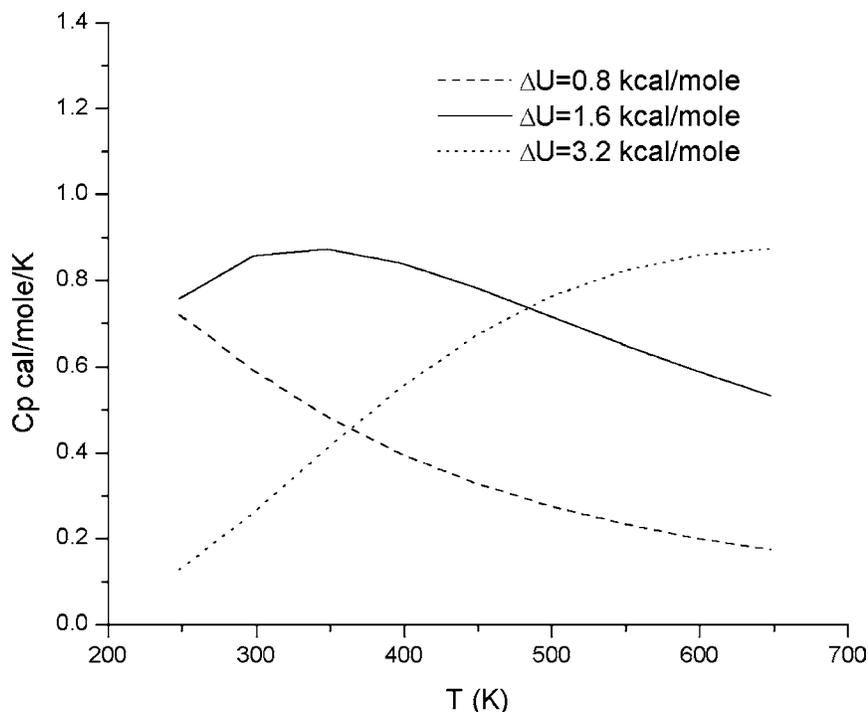
**Figure 2** Effect of temperature on heat capacity in a two-energy-level system.

Figures 2 and 3 show the effect of temperature on the heat capacity in the two-energy-level model. Increasing  $T$  simply has the effect of scaling the energy axis uniformly. However, the direction of the effect on  $C_p$  depends on whether we are above or below the critical energy gap value. With larger gaps, increasing the temperature increases  $C_p$ . With smaller gaps, increasing  $T$  decreases  $C_p$ . Thus depending on where the system is relative to the critical energy gap value and the accessible temperature range,  $C_p$  may appear to increase monotonically, decrease monotonically, or exhibit a maximum (Figure 3).

In Figure 4, the effect on the heat capacity of increasing the degeneracy of the upper level to  $N = 2, 4, 8, 16$ , etc., is plotted. Here the more general expression for  $C_p$  in the two-energy-level model is

$$C_p = \frac{\Delta U^2 N e^{-\Delta U/kT}}{kT^2(1 + N e^{-\Delta U/kT})^2} = \frac{\Delta U^2}{kT^2} p_0 p_1, \quad 16.$$

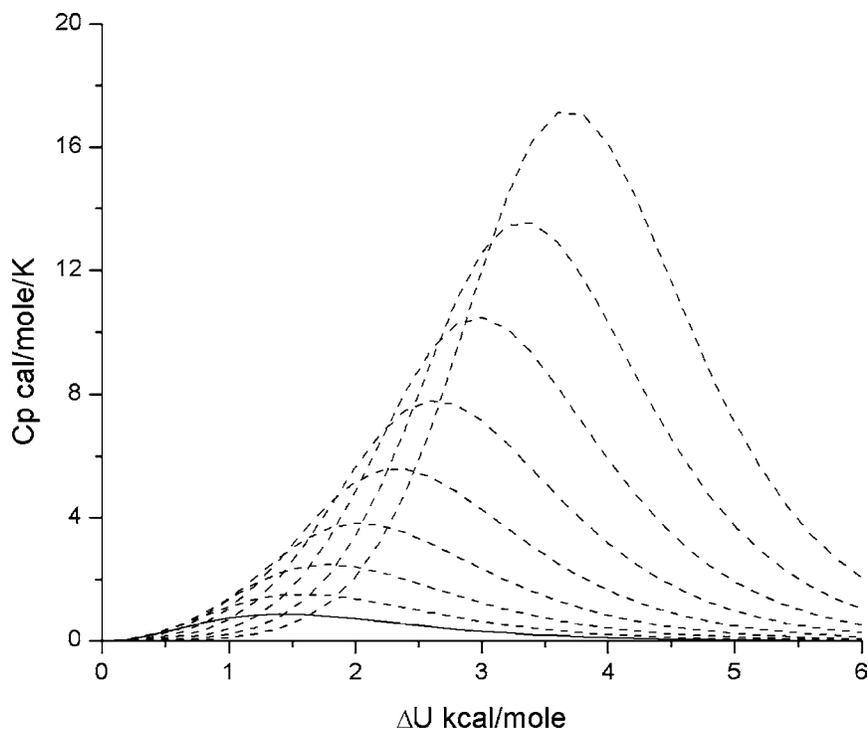
where now  $p_1$  is the probability of occupying any of the upper energy levels. For large energy gaps,  $C_p$  increases almost linearly with  $N$ , hence the qualitative description of  $C_p$  as a measure of the number of thermally accessible high energy states. For a low energy gap the situation is more complex. With increasing  $N$ ,  $C_p$



**Figure 3** Temperature profile of  $C_p$  for a two-energy-level system.

increases then decreases. This again is best understood in terms of the enthalpy fluctuation definition. As the degeneracy (entropy) of the higher energy state is increased, at first  $C_p$  increases as the factor  $p_0 p_1$  increases. Eventually as  $N$  increases, the system spends most of its time in the upper energy states,  $p_0 \ll 1$ , and the energy fluctuation decreases. With increasing  $N$ , both the position and the height of the maximum in  $C_p$  increases. From this one might say, using the language of entropy-enthalpy compensation, that the maximum  $C_p$  is achieved when the effect of degeneracy and energy gap balance, i.e., when there is the right balance of a “low energy, low entropy” ground state, and a “high entropy, high energy” upper state.

To summarize the points emerging from simple models of heat capacity, the magnitude of  $C_p$  is determined by a balance between fluctuations of the systems between different states, which is large when their energy gap is small, and the energy changes occurring upon transition between these states, which is large when the energy gaps are large. The nonmonotonic dependence of  $C_p$  on energy gap, temperature, and energy level degeneracy makes interpretation of  $C_p$  changes more difficult than that of entropy, for example. In this regard, it is usually easier to think of  $C_p$  in terms of energy fluctuations rather than of temperature derivatives of  $H$ ,  $S$ ,



**Figure 4** Effect of upper energy level degeneracy,  $N$ , on heat capacity. *Solid line:*  $N = 1$ . *Dashed lines* indicate successive doubling of  $N$  to 2, 4, 8, 16, 32, 64, 128, and 256.

or the other definitions of  $C_p$ . We can also identify two general regimes: a regime where the energy gap(s) between the most probable states are large, characterized by an increase in  $C_p$  with temperature, and a small energy gap regime where  $C_p$  decreases with increasing  $T$ . Experimental determination of the dependence of  $C_p$  on  $T$  can thus provide some general information on the protein energy landscape. The reader is referred to the elegant work of Poland (10, 11) for a more detailed exposition of the relationship between heat capacity and protein energy landscapes.

### 3. SOME IMPLICATIONS OF OBSERVED $C_p$ CHANGES IN PROTEINS

The multiple definitions for heat capacity probably make for a richer set of consequences than for any of the other four major thermodynamic quantities— $G$ ,  $H$ ,  $S$ , and  $V$ —usually measured for proteins. Some of the more intriguing

consequences are summarized below and discussed in more detail in separate sections.

- i. The sign of  $\Delta C_p$  distinguishes apolar (+) from polar (–) solvation (3, 4, 12, 13), in contrast to  $\Delta S$  and  $\Delta H$  of hydration, which are both negative for apolar and polar groups. Indeed, a positive  $\Delta C_p$ , rather than negative  $\Delta S$ , is now considered the signature of the hydrophobic effect. Thus, from Equations 1 and 2a, polar and apolar groups buried in protein folding and binding impart different temperature dependences to the entropy and enthalpy of these processes, to the extent that, depending on the mix of apolar/polar groups involved, a process may switch from being entropy driven at one temperature to enthalpy driven at another, or dominated by apolar interactions at one temperature and polar interactions at another.
- ii. Solvation of polar groups found in proteins is characterized by both negative  $\Delta C_p$  and  $\Delta S$  at room temperature (14, 15). Therefore one can infer from Equation 2a that the entropy of hydration becomes more negative as the temperature is raised, i.e., that, at least in this temperature range, there is increased structuring of water by the solute at higher temperature. This is indeed counterintuitive.
- iii. Globular protein unfolding usually has a positive  $\Delta C_p$ . From Equation 2b one can infer that the stability versus temperature profile has an inverted U-shape. Indeed, many proteins have a maximum in stability, often close to their normal ambient temperature. In addition to the expected decrease in stability with increasing temperature (the familiar melting transition), the downward curve in stability imparted by a positive  $\Delta C_p$  implies that proteins become less stable at low temperature and can even denature at low enough temperatures (3, 16, 17). The temperature-stability profile, and thus the heat capacity of unfolding also, has important implications for the mechanism of stabilization of thermophilic and hyperthermophilic proteins that function at temperatures of 60–120°C (18–20).
- iv. Base sequence-specific binding of proteins to DNA is usually accompanied by a very large decrease in  $C_p$ , whereas nonspecific binding is not (21–24). This difference is increasingly seen as the thermodynamic signature of sequence-specific recognition. The large decrease in enthalpy fluctuations produced by sequence-specific binding, deduced from Equation 2c, is largely unexplained, but it may reflect large changes in DNA dynamics.

#### 4. $C_p$ CHANGES AND MEASUREMENT OF PROTEIN ENTHALPY

Although  $C_p$  changes in proteins are themselves of considerable interest, they can also complicate the measurement of enthalpy. Enthalpy changes can be measured directly by calorimetric techniques such as ITC for binding and DSC for melting.

One can also obtain a calorimetric measurement of  $\Delta C_p$ , for example, from ITC measurements at different temperatures using Equation 1. The alternative approach is to obtain  $\Delta H$  and  $\Delta C_p$  from the temperature dependence of the equilibrium constant or  $\Delta G$ , through the van't Hoff equation for enthalpy

$$\Delta H = \frac{\partial \Delta G/T}{\partial 1/T}, \quad 17.$$

and fitting to the integrated van't Hoff equation (Equation 12c) for  $\Delta C_p$ . Differences between calorimetric and van't Hoff measurements of enthalpy have been consistently observed for a number of protein systems (25, 26) to the extent that theoretical justifications for such differences were proposed, including radical reinterpretations of DSC curves (27) and questioning of the van't Hoff Equation (28). Attempts to provide theoretical reasons for the discrepancies have focused on the statistical mechanical definition and physical interpretation of heat capacity. Equation 17 says that, in principle, the enthalpy can be obtained from just the slope of  $\Delta G/T$ . In practice, reliable determination of the slope requires measurement over an appreciable temperature range, and one must therefore account for the temperature dependence of  $\Delta H$  imparted by any heat capacity change. Thus,  $\Delta H$  is usually obtained from Equation 12c simultaneously with  $\Delta C_p$  by fitting. Chaires (29) has analyzed in depth correlations in errors between  $\Delta C_p$  and  $\Delta H$  inherent in this fitting that account in large part for spurious differences in calorimetric and van't Hoff enthalpies. This analysis also emphasizes the need for many more data points for reliable fitting of  $\Delta G$  versus  $T$  than are typically used. In addition, a comparison of Equations 12c and 13 shows that neglect of the temperature dependence of  $C_p$  itself will likely result in further systematic deviation of the van't Hoff enthalpy from the calorimetric value. Moreover, even more temperature measurements should be used for van't Hoff fitting. Other authors agree with the assessment that differences in the two estimates result from measurement/fitting inadequacies, and vigorously rebut any theoretical justification for the discrepancies (30, 31).

## 5. LINKED EQUILIBRIA AND HEAT CAPACITY CHANGES

In an influential paper, Eftink & Biltonen laid out the implications of linked equilibria for the measurement of thermodynamic parameters on proteins (32). In summarizing the part of their analysis relevant to heat capacity, consider a protein with two conformations A and B in equilibrium described by the constant  $K_{ab} = [B]/[A]$ , and a ligand L that can only bind the B-form with affinity constant  $K_L = [BL]/[B][L]$ . The net binding equilibrium is given by

$$K_{net} = \frac{[BL]}{[L]([A] + [B])} = \frac{[BL]}{[L][B](1 + 1/K_{ab})} = K_L f_b, \quad 18.$$

where  $f_b$  is the fraction of the protein in the B-form in the absence of ligand. Taking  $\Delta G_{net} = -kT \ln K_{net}$  and using Equation 2b, the expression for the heat

capacity is

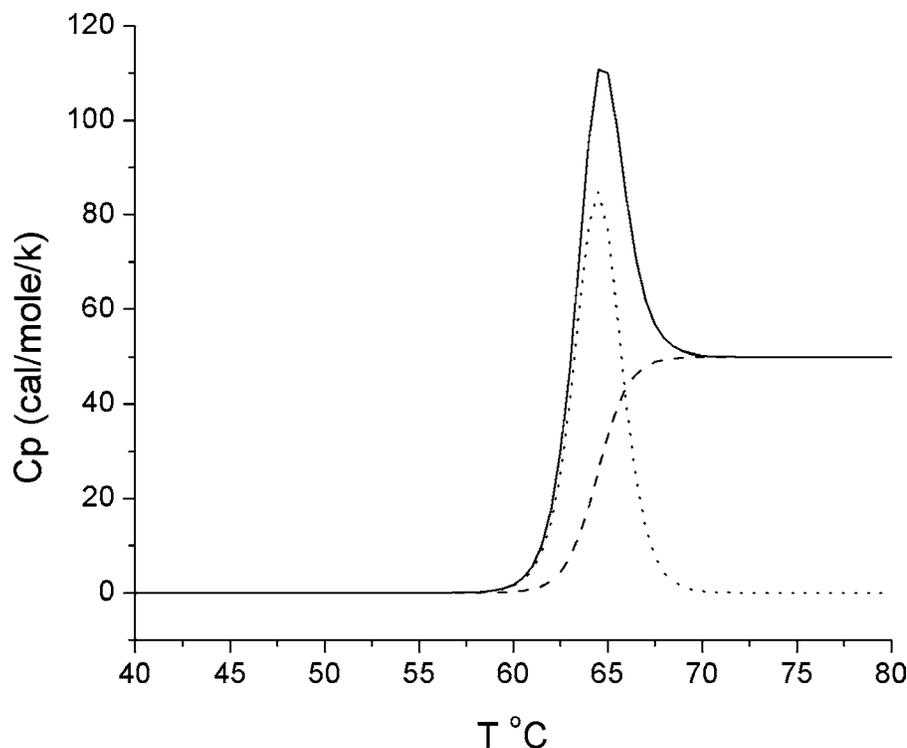
$$\Delta C p^{net} = \Delta C p^L + \Delta C p^{ab} f_a - \frac{\Delta H_{ab}^2}{kT^2} f_a f_b, \quad 19.$$

where  $f_{ac} = 1 - f_b$  is the fraction of the protein in the A-form in the absence of ligand. The first term in Equation 19 is the intrinsic heat capacity of ligand binding. The second term is the intrinsic heat capacity for converting the fraction of protein in the A-form to the B-form so that L can bind. The third term has no connection with the intrinsic heat capacities of either the protein or its interaction with the ligand. It arises purely from the link in protein conformational equilibrium with the binding. In the absence of ligand, the protein fluctuates between two forms with different energy, but when bound to the ligand it is constrained to the B-form, resulting in a loss of this heat capacity contribution (note the analogous form of this term to Equation 15). Such a contribution to heat capacity is often referred to as apparent (i.e., it is apparently not what the experimentalist was hoping to measure!), although it is as real and as measurable as both the intrinsic contributions. Adopting the statistical mechanical perspective, we can see that this contribution arises as the system fluctuates between the “states” A+L, B+L, and BL, each with a different average energy, while “intrinsic” Cp contributions arise from fluctuations in energy levels within the states A, B, or L. All Cp contributions are the same in the sense that they simply reflect fluctuations between states of different energy.

An important point emerging from this analysis is that if the linked equilibrium is of the type where the ligand binds predominantly to one form (mandatory coupling in the language of Eftink & Biltonen), then this heat capacity contribution is always negative irrespective of which conformation (A or B) has the lower energy. It is also present even if the intrinsic heat capacity changes are zero. It is therefore interesting that this term has the right sign to explain in part the unexpectedly large negative heat capacity changes that accompany base sequence-specific binding of proteins to DNA (21–24). This explanation assumes a protein binding-linked perturbation of some conformational equilibrium in the DNA. (If the observed Cp effect was positive one could immediately rule out this kind of explanation.)

The fluctuation of a protein between two states is also responsible for the peak in Cp seen in DSC melt curves (33) (Figure 5). The excess or conformational fluctuation heat capacity is given by  $\Delta H_{ND}^2 f_N f_D / kT^2$ , where  $\Delta H_{ND}$  is the difference in enthalpy between, and  $f_N, f_D$  are the fractions of, the native and denatured states. Both states are appreciably populated during the melting transition. In this case, integration of the excess Cp over T is used to extract the unfolding enthalpy.

When imparting a heat capacity to a process, linked equilibrium effects can complicate extraction of enthalpies by van't Hoff analysis and produce the apparent discrepancy with calorimetric values discussed above. In a systematic evaluation of this effect, Horn et al. (34, 35) have shown, using some of the same protein systems previously thought to show systematic differences, that within experimental error van't Hoff and calorimetric enthalpy estimates agree. Their analysis also describes



**Figure 5** Model DSC trace for protein melting, generated using  $\Delta H = 80$  kcal/mol,  $\Delta S = 0.2$  kcal/mol/K, and  $\Delta C_p = 50$  cal/mol/K for unfolding at  $T = 298$  K, and Equation 12.  $\Delta C_p^{\text{fluc}} = \Delta H^2 f_N f_D / kT$  ( $\cdots$ ),  $\Delta C_p^{\text{ND}} = f_D \Delta C_p$  ( $---$ ), and  $C_p^{\text{tot}}$  ( $—$ ).

contributions to the putative discrepancies from linkage to proton exchange with buffer and protein-ion binding. These discrepancies are particularly insidious, as the proton and ion equilibria are usually invisible to the techniques commonly used to measure protein binding and unfolding. In summary, careful analyses of calorimetric-van't Hoff discrepancies of the type described in this and the preceding sections show that they can be attributed to measurement artifacts or incorrect assumptions in the model of analysis, and indeed there is no sound theoretical reason to expect them to differ (30, 31).

## 6. SEPARATION OF HEAT CAPACITY COMPONENTS

In analysis of the thermodynamics of complex systems such as proteins, a widespread and extremely useful practice is to divide net changes in  $G$ ,  $H$ ,  $S$  or  $C_p$  into components reflecting either different physical contributions (e.g., electrostatic,



## 7. GROUP ADDITIVITY, HEAT CAPACITY, AND TEMPERATURE CONVERGENCE OF ENTROPY AND ENTHALPY CHANGES

Starting with the findings of Sturtevant (45) that in certain solvation processes the ratio  $\Delta S/\Delta C_p$  is approximately constant at 25°C, Baldwin made the key observation that a linear relationship between  $\Delta S$  and  $\Delta C_p$  implied convergence of entropy values for hydrophobic group solvation at a unique temperature,  $T^s \approx 112^\circ\text{C}$  (13). This behavior was initially observed for homologous series of model solutes containing hydrophobic groups, such as inert gases and linear alkanes.

To understand this convergence behavior, consider such a series of compounds where the entropy change is linearly related to the heat capacity change, as  $\Delta S = a_s \Delta C_p + b_s$  at a given temperature  $T^{\text{ref}}$ . Substituting into the van't Hoff relation Equation 12b, for a given compound  $i$

$$\Delta S^i = b_s + \Delta C_p^i [a_s + \ln(T/T^{\text{ref}})]. \quad 24.$$

At the convergence temperature of  $T^s = T^{\text{ref}} e^{-a_s}$ , the entropy change is  $\Delta S^i = b_s$ , i.e., it is identical for all compounds in the series. Experimental data show that for hydrophobic solutes such as inert gases and linear alkanes,  $b_s$  is also close to zero. Similarly, if  $\Delta H = a_h \Delta C_p + b_h$ , then

$$\Delta H^i = b_h + \Delta C_p^i [a_h + (T - T^{\text{ref}})], \quad 25.$$

and at  $T^h = T^{\text{ref}} - a_h$ ,  $\Delta H^i = b_h$ . Expressed as plots of  $\Delta S$  or  $\Delta H$  versus  $T$  the convergence behavior described by Equation 24, 25 produces a series of lines, one for each compound, that cross at a single temperature (3). For homologous solutes, group additivity or scaling behavior provides the simplest explanation for this behavior. As homologous groups are added to a compound, or as a homogenous solute such as a linear alkane or inert gas is increased in size, one expects a linear change in all the usual extensive thermodynamic hydration quantities,

$$\Delta X^i = p_X + q_X Q^i, \quad 26.$$

where  $\Delta X = \Delta S, \Delta H, \Delta C_p$ , etc., and  $p_X$  and  $q_X$  are coefficients describing the linear behavior of quantity  $X$ .  $Q^i$  represents the size of the  $i^{\text{th}}$  solute in terms of a physical dimension or number of homologous groups as appropriate. Eliminating  $Q^i$  between pair of such linear size or scaling equations leads straightforwardly to linear relationships between  $C_p$  and  $S$  or  $H$ , and hence to convergence behavior for small solutes. Such scaling is the basis for explanations of convergence behavior from several studies of solutes (15, 16, 46, 47). In addition, as Murphy and coworkers have pointed out, the coefficients  $a$  and  $b$  are themselves valuable in that they enable the contribution of the constant to be separated out from the varying parts of a homologous solute series (12, 16).

Given the additivity/scaling explanation of convergence for homologous solutes, it was remarkable that convergence behavior was subsequently found for

unfolding a set of small globular proteins, for both enthalpy and entropy, when normalized by the number of residues (12). Moreover, for entropy,  $T^s$  was close to that of hydrophobic solutes. This surprising result has sparked considerable interest and ongoing debate on the dependence of the hydrophobic effect on temperature and the role of hydrophobic stabilization in proteins at physiological and higher temperatures (13, 14, 46–52). To highlight just a few issues that have emerged, consider the two observations that  $T^s$  is similar for hydrophobic solutes and these proteins, and that for the former,  $b_s$  is close to zero (i.e., at about 112°C the entropy of apolar hydration is close to zero). First, this shows that, due to the large positive hydration  $C_p$  characteristic of hydrophobic solvation, close to and above  $T^s$ , the hydrophobic effect is dominated by unfavorable enthalpy, not by unfavorable entropy. Second, it implies a universal behavior for the hydration entropy of hydrophobic solutes. Third, it raises the possibility that by measuring or calculating the entropy of protein unfolding at  $T^s$  and then extrapolating back to ambient temperatures using the van't Hoff relations, one can cleanly separate out one contribution (apolar hydration entropy) to protein stability. This is a rare and tantalizing possibility for thermodynamic measurements on such complex systems as proteins. This kind of extrapolation and dissection has been used to good effect in the parameterization of empirical energy functions for proteins (53–55).

The dominant role of hydrophobic interactions in protein stabilization was a common theme in the different explanations proposed for entropy and enthalpy convergence behavior in proteins referenced above. However, in an extensive analysis of protein unfolding thermodynamics that includes many more proteins, Robertson & Murphy have shown that the evidence for convergence behavior in  $\Delta S$  and  $\Delta H$  of unfolding is not compelling, i.e., plots of these quantities against  $\Delta C_p$  of unfolding show little evidence of linearity (16). Interestingly, the thermodynamics of hydrophobic hydration has now been invoked to explain the *scatter* in the  $\Delta S/\Delta C_p$  plots (52). Thus, as a large group, proteins do not act as a set of homologous compounds (when normalized by their size) but smaller, more related sets of proteins may.

## 8. CONTRIBUTIONS TO $C_p$ IN PROTEINS

An influential study by Sturtevant (45) listed most of the possible sources of  $C_p$  changes in protein unfolding ( $\Delta C_p^{\text{unfold}}$ ) and binding; these include the hydration of hydrophobic groups, hydrogen bonding, electrostatics, and protein conformational entropy, vibrational terms, and changes in equilibrium (i.e., the linked equilibrium effect described above). More than 25 years later, this remains predominantly a list. The exception is the polar and apolar hydration contributions, which have been fairly accurately quantified for protein unfolding mostly due to systematic measurements on model compounds and peptides (4, 5, 14, 15, 43, 44). The magnitude, importance, and even the sign of the other terms remain uncertain. Reasons for this uncertainty include absence of suitable model systems, difficulty

in extracting specific contributions from measured net  $C_p$  changes, and the inherent difficulties in simulating or developing theoretical models for a higher-order derivative/fluctuation quantity like  $C_p$  in molecular detail for large molecules such as proteins. Most current work has therefore addressed the contributions to protein  $C_p$  changes with a much broader division: into hydration versus nonhydration, i.e., protein terms. To put this into the framework of the separability of  $C_p$  components described by Equation 22, the net enthalpy change in a protein unfolding or binding reaction can be divided up as

$$\Delta H = \Delta H^{\text{protein-protein}} + \Delta H^{\text{protein-solvent}} + \Delta H^{\text{solvent-solvent}}, \quad 27.$$

with corresponding  $\Delta C_p$  contributions,

$$\begin{aligned} \Delta C_p &= \Delta C_p^{\text{protein-protein}} + (\Delta C_p^{\text{protein-solvent}} + \Delta C_p^{\text{solvent-solvent}}) \\ &= \Delta C_p^{\text{protein-protein}} + \Delta C_p^{\text{hydration}} \end{aligned}$$

The solvent-solvent term arises because of protein-solvent interactions, and both involve solvent so they can be grouped into a single hydration term. The relative size of these two terms is not known in general, but from a molecular dynamics study of Xenon in water (56), the solvent-solvent contribution to  $C_p$  is about an order of magnitude higher than the solute-solvent interaction, which is consistent with the general view that for hydrophobic compounds, the water-water interaction is the dominant term. Debate about the relative importance of  $C_p$  contributions, summarized below, centers around whether the  $C_p$  increase upon protein unfolding can mostly or completely be accounted for by hydration effects or whether there are significant internal protein conformations, i.e., what are the relative sizes of  $\Delta C_p^{\text{protein-protein}}$  and  $\Delta C_p^{\text{hydration}}$ .

### 8.1. Is Protein Unfolding $C_p$ in Proteins Dominated by Hydration or by Protein-Protein Interactions?

For protein unfolding, hydration effects are clearly significant; early evidence showed that hydration is the major effect (57). The strongest current evidence is that one can account for  $\Delta C_p^{\text{unfold}}$  for many proteins by adding up hydration contributions from individual groups (58–61). Indeed, the prevalent use of area models (see below) to analyze protein  $C_p$  data is based on this assumption. However, the protein data themselves are insufficient to clinch the argument; Robertson & Murphy's analysis shows that the data can be equally well fit by a number of area-based hydration models (16). This variability may also reflect overestimation of how unfolded the protein is in the denatured state (61–63), which factors into the correct calculation of area changes. Also, recent measurement of changes in  $\Delta C_p^{\text{unfold}}$  due to point mutations shows that the direction is consistent with the hydration effect but sometimes fivefold larger (64). Assessment of the nonhydration contributions to  $\Delta C_p^{\text{unfold}}$  is difficult, but Dadarlat & Post (65) found that  $\Delta C_p^{\text{unfold}}$  increased with compressibility of the native state protein. This increase



estimates. However, this improvement could be interpreted either as a better treatment of area hydration or as evidence of an effect of S–S bonds on the protein conformational contribution to  $\Delta C_p^{\text{unfold}}$ .

Although the contribution of DNA to protein-DNA binding  $C_p$  changes is beyond the scope of this review, we note that for specific base protein-DNA binding where coupled protein folding and binding is not involved, e.g., BamHI (23, 24), one cannot account for the large negative  $C_p$  changes with any reasonable hydration model. Thus, binding-related damping of DNA internal fluctuations very likely contributes significantly to  $C_p$ . However, it is still an open question as to whether protein conformational fluctuations, or any other  $\Delta C_p^{\text{protein-protein}}$  term, is comparable to the  $\Delta C_p^{\text{hydration}}$  term for folding and protein-protein binding.

## 9. THEORETICAL MODELS FOR $C_p$ CONTRIBUTIONS IN PROTEINS

We can broadly identify two heat capacity contributions in proteins,  $\Delta C_p^{\text{protein-protein}}$  and  $\Delta C_p^{\text{hydration}}$ . What can be said about the physical origins, in molecular and atomic terms, of each of these? The experiments have given us mostly thermodynamic data, and from thermodynamics one cannot infer mechanisms. Thus the answer lies in what physical models, or simulation methodologies, are available to calculate  $C_p$  contributions and compare with experiment. As mentioned above, there are almost no atomic level treatments of heat capacity at the level of whole proteins, and there are unlikely to be any in the near future. Simulation technology has advanced to the point where free energy changes can be obtained for proteins, but with considerable computational effort and usually for rather small changes, i.e., point residue mutations. Entropy can be extracted from such simulations for similar size changes, but with even more effort. Thus to extract, for example, a higher-order fluctuation/derivative quantity like  $C_p$ , and for a large-scale change such as unfolding, is difficulty squared. Atomic detail theoretical models and simulations of heat capacity relevant to proteins are thus almost entirely confined to treatment of the hydration term, usually studied on protein constituents or model compounds. The aim has been to account for the major  $C_p$ -related features of hydration:

- i. The positive  $C_p$  of hydration for apolar groups;
- ii. The negative  $C_p$  of hydration for polar groups;
- iii. The convergence of apolar group hydration at  $T \approx 112^\circ\text{C}$ ;
- iv. For apolar groups the switch from negative entropy, enthalpy of hydration at room temperature to positive entropy, enthalpy of apolar hydration above the convergence temperature (this regime is still relevant to the biology of protein stability because proteins from hyperthermophiles function at these temperatures);
- v. The decrease in apolar hydration  $C_p$  with increasing temperature; and

- vi. The temperature maximum in stability that most proteins exhibit, and the cold-induced denaturation that some proteins can be made to undergo.

An additional important goal has been to develop practical but accurate models for use on large protein and DNA systems to calculate  $\Delta C_p^{\text{hydration}}$  for binding and unfolding.

### 9.1. Area-Based Models for Hydration $C_p$

One of the simplest, but most widely used, models for calculating hydration heat capacity in proteins is the solvent-accessible surface area model. Careful measurements on model compound and protein data (4, 5, 14, 15, 43, 44) show unequivocally that hydration of apolar and polar groups is accompanied by increases and decreases in  $C_p$ , respectively. For the model compound data, these changes are to a good approximation proportional to the changes in apolar and polar solvent-accessible area,  $\Delta A_n$  and  $\Delta A_p$ . Similar relations apply to the protein data, where Makhatadze & Privalov (4, 5) analyzed  $C_p$  contributions from backbone and side chains. They found nonpolar  $\Delta C_p^{\text{hydration}}$  is positive at low temperature, and decreases with increasing temperature, whereas for polar groups it is negative at low temperature.  $\Delta C_p^{\text{hydration}}$  of side chains correlated well with surface area. These and other studies led to the area model hydration heat capacity equation

$$\Delta C_p^{\text{hydration}} = C_n \Delta A_n + C_p \Delta A_p.$$

This equation is easy to apply to protein systems, although, as mentioned above, calculation of unfolded state areas has uncertainties. This equation is also the basis for a general and extremely versatile total protein energy function used to study conformational aspects of proteins (54, 71, 72). However, depending on the data sets used to derive the coefficients, a variety of values for  $C_n$  and  $C_p$  have been obtained (Table 1). In many applications, these give very similar results (64), albeit with variations. In the most extensive analysis of protein data to date, Robertson & Murphy pointed out that the  $C_p$  data can be fit equally well with a number of area models (owing to the variability and complexity of the proteins, and attendant  $C_p$

**TABLE 1** Area coefficients for hydration heat capacity equation<sup>a</sup>

Source	Data set	$C_n$	$C_p$
Spolar et al. (59)	12 proteins	1.34	-0.59
Murphy & Friere (101)	Cyclic dipeptides	1.88	-1.09
Myers et al. (61)	26 proteins	1.17	-0.38
Makhatadze & Privalov (58)	20 proteins	2.14	-0.88
Robertson & Murphy (16)	49 proteins	0.66	0.52
Sharp & Madan (73)	Nucleic acid fragments	0.71	0.71

<sup>a</sup>For the equation  $\Delta C_p^{\text{hydration}} = C_n \Delta A_n + C_p \Delta A_p$ , values in J/mol/K/Å<sup>2</sup>.

measurement uncertainties). This points to the limitation in using protein data alone and the importance of using model compound data (16). These protein coefficients have also been used, for want of any alternative, to compute the contribution to  $\Delta C_p^{\text{bind}}$  from burial of DNA surface by proteins in an attempt to explain large base sequence-specific decreases in  $C_p$  (60). However, more recent work on nucleic acid model compounds, which also provides preliminary coefficients for the area model (Table 1) (73), shows that hydration of nucleic acids is quite different, and that use of protein values will lead to large errors in  $\Delta C_p^{\text{hydration}}$ . Finally, these area models, though useful, are entirely empirical, and shed no light on why the hydration  $C_p$ s of polar and apolar groups have the sign and magnitude they do.

## 9.2. Two-State Models for Hydration $C_p$

Extending an earlier two-state model (74), Muller (75) developed a simple but influential two-water-state model to explain the increase in  $C_p$  upon hydrating apolar groups. The two states are made and broken water H-bonds, which are in equilibrium. H-bond breaking is characterized by positive enthalpy and entropy changes, changes that are different in bulk water and in the solute hydration shell. The model thus needs four thermodynamic parameters, which are obtained from thermodynamic data on water and fitting. The result satisfactorily reproduces the positive  $\Delta C_p^{\text{hydration}}$  for apolar solute solvation, and even the observed decrease in  $\Delta C_p^{\text{hydration}}$  with increasing  $T$ . The model has subsequently been generalized (76). Referring to additional experimental rationales for treating water as a mixture of two or more distinct states (77), Silverstein et al. recently refined the model further (6), using better data on water. This refinement has improved the fit to the temperature dependence of  $\Delta C_p^{\text{hydration}}$  of inert gases. In the context of a two-state model, an interesting inference that can be drawn from the observed decrease of  $\Delta C_p^{\text{hydration}}$  with increasing  $T$  is that hydrophobic solvation at room temperature occurs in a low energy gap regime (Figure 3).

However, with both original and refined parameter values, the Muller model gives a positive entropy and enthalpy of solvation of apolar groups at room temperature, opposite to experiment. Muller's original intent was to explain  $C_p$  changes with his model. The original paper apparently shows the correct direction of  $S$  and  $H$  changes, but there is an error in both entropy and enthalpy expressions, although not with the  $C_p$  expression.

Bakk et al. (78, 79) have made an interesting extension to the two-state model for  $C_p$  hydration, adding an extra term from immobilization of water by H bonded around polar groups to treat the polar contribution too. They have applied this extension to proteins, where it produces  $\Delta G^{\text{unfold}}$  versus  $T$  profiles with magnitude and curvature similar to those of protein data, exhibiting both melting and cold denaturation behavior.

## 9.3. Statistical Mechanical Models for Hydrophobic Solvation

Statistical mechanical and atomic level simulation studies of solute hydration are too numerous to summarize here, and we focus on a subset that













